H-Functions are working horses in cryptography.

A cryptographic hash function is a special class of hash function that has certain properties which make it suitable for use in cryptography. It is a mathematical <u>algorithm</u> that <u>maps</u> data of arbitrary size to a <u>bit string</u> of a fixed size (a hash function) which is designed to also be a one-way function, that is, a function which is infeasible to invert.

The only way to recreate the input data from an ideal cryptographic hash function's output is to attempt a brute-force search of possible inputs to see if they produce a match.

Bruce Schneier has called one-way hash functions "the workhorses of modern cryptography".

The input data is often called the *message*, and the output (the *hash* value or hash) is often called the message digest or simply the digest.

M-message h = H(m)m- of finite length In = 256 Bits h = 28 Rits = 7 hexnumb.

 $OOOO_{h} = O_{h} \equiv O_{d}$ 0001b = 1h= 1d

 $0010_{h} = 2_{h} = 2_{d}$

1001 = 910 = 910

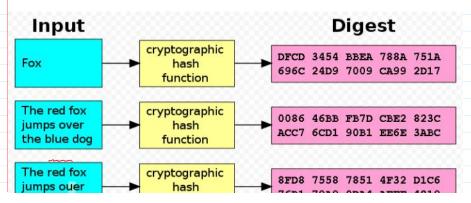
1010 = A16 = 10,0

1110 = Eh = 140 1111 = Fh = 1510

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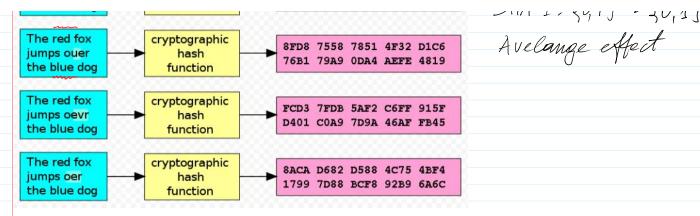
1) When given
$$m$$
 and $H()$, then it is easy to compute $h = H(m)$.
2) It is infeasible to find any m' such that $H(m') = h$.

Cryptographic hash functions have many information-security applications, notably in digital signatures, message authentication codes (HMACs), and other forms of authentication. They can also be used as ordinary hash functions, to index data in hash tables, for fingerprinting, to detect duplicate data or uniquely identify files, and as checksums to detect accidental data corruption. Indeed, in information-security contexts, cryptographic hash values are sometimes called (digital) fingerprints, checksums, or just hash values, even though all these terms stand for more general functions with rather different properties and purposes.



40 Hex numbers = 160 bits

SHA-1 SHA-1: {0,1}* - {0,1}160 Avelange effect



A cryptographic hash function (specifically <u>SHA-1</u>) at work. A small change in the input (in the word "over") drastically changes the output (digest). This is the so-called avalanche effect.

Properties

- it is quick to compute the hash value for any given message.
- a small change to a message should change the hash value so extensively that the new hash value appears uncorrelated with the old hash value.

Most cryptographic hash functions are designed to take a <u>string</u> of any finite length as input and produce a fixed-length hash value.

A cryptographic hash function must be able to withstand all known types of cryptanalytic attack.

In theoretical cryptography, the security level of a cryptographic hash function has been defined using the following properties:

• Pre-image resistance

Given a hash value h it should be difficult to find any message m' such that h = H(m') = hash(m'). This concept is related to that of <u>one-way function</u>. Functions that lack this property are vulnerable to <u>preimage attacks</u>.

• Second pre-image resistance

Given an input m_1 it should be difficult to find (different) input m_2 such that $hash(m_1) = hash(m_2)$.

Functions that lack this property are vulnerable to second-preimage attacks.

Collision resistance

It should be difficult to find $\frac{any}{any}$ two different messages m_1 and m_2 such that $hash(m_1) = hash(m_2)$. Such a pair is called a cryptographic $\frac{hash}{any}$ collision. This property is sometimes referred to as strong collision resistance. It requires a hash value at least twice as long as that required for preimage-resistance; otherwise $\frac{collisions}{any}$ may be found by a $\frac{birthday}{any}$ attack.

These properties form a hierarchy, in that collision resistance implies second pre-image resistance, which in turns implies pre-image resistance, while the

 m_1 - contract $H(m_1) = h_1$ $Sig(h_1) = S_1$ $m_2 = 100000 \in$ $H(m_1) = H(m_2)$ SHA - 256 These properties form a hierarchy, in that collision resistance implies second pre-image resistance, which in turns implies pre-image resistance, while the converse is not true in general. [3]

SHA - 256
64 Hex digits
sha 256 (9 - - - 7)

The weaker assumption is always preferred in theoretical cryptography, but in practice, a hash-functions which is only second pre-image resistant is considered insecure and is therefore not recommended for real applications. Informally, these properties mean that a <u>malicious adversary</u> cannot replace or modify the input data without changing its digest.

Thus, if two strings have the same digest, one can be very confident that they are identical.

Checksum algorithms, such as <u>CRC32</u> and other <u>cyclic redundancy checks</u>, are designed to meet much weaker requirements, and are generally unsuitable as cryptographic hash functions.

For example, a CRC was used for message integrity in the <u>WEP</u> encryption standard, but an attack was readily discovered which exploited the linearity of the checksum.

Illustration

>> sha256('RootHash PrevHash 73732763<mark>1</mark>')
ans = F4AE534CD226FAF799 8C8424B348E020BA80639A687E93A0B8C5130EDC51E6DE
>> sha256('RootHash PrevHash 73732763<mark>2</mark>')

ans = B856211DF2EE15E30AB770C1A43CE014ECFE573182AFD885B28D96854DBC5F21
>> sha256('RootHash PrevHash 73732763<mark>3</mark>')
ans = 9C18C764E347A58E57AC3F7A3C2874D5889A0E802699FEA47EEFF8C03BFEDA69

2100704234773023776317730207423003702002033127472211100032122703

$$O_{h} = 0000_{2}$$
; $F_{h} = 1111_{2}$

Commitment

An illustration of the potential use of a cryptographic hash is as follows: Alice poses a tough math problem to Bob and claims she has solved it. Bob would like to try it himself, but would yet like to be sure that Alice is not bluffing.

P = NP $P \neq NP$

Therefore, Alice writes down her solution, computes its hash and tells Bob the hash value (whilst keeping the solution secret).

Then, when Bob comes up with the solution himself a few days later, Alice can prove that she had the solution earlier by revealing it and having Bob hash it and check that it matches the hash value given to him before. (This is an example of a simple commitment scheme; in actual practice, Alice and Bob will often be computer programs, and the secret would be something less easily spoofed than a claimed puzzle solution).

Verifying the integrity of files or messages

Main article: File verification

 $m \pm m$

Verifying the integrity of files or messages

Main article: File verification

An important application of secure hashes is verification of message integrity. Determining whether any changes have been made to a message (or a file), for example, can be accomplished by comparing message digests calculated before, and after, transmission (or any other event).

For this reason, most <u>digital signature</u> algorithms only confirm the authenticity of a hashed digest of the message to be "signed". Verifying the authenticity of a hashed digest of the message is considered proof that the message itself is authentic.

MD5, SHA1, or SHA2 hashes are sometimes posted along with files on websites or forums to allow verification of integrity. [6] This practice establishes a chain of trust so long as the hashes are posted on a site authenticated by HTTPS.

 $m \neq m'$ $h = H(m) \neq h' = H(m')$

SHA-256

Password verification[edit]

Main article: password hashing

A related application is <u>password</u> verification (first invented by <u>Roger Needham</u>). Storing all user passwords as <u>cleartext</u> can result in a massive security breach if the password file is compromised. One way to reduce this danger is to only store the hash digest of each password. To authenticate a user, the password presented by the user is hashed and compared with the stored hash. (Note that this approach prevents the original passwords from being retrieved if forgotten or lost, and they have to be replaced with new ones.) The password is often concatenated with a random, non-secret <u>salt</u> value before the hash function is applied. The salt is stored with the password hash. Because users have different salts, it is not feasible to store tables of <u>precomputed</u> hash values for common passwords. <u>Key stretching</u> functions, such as <u>PBKDF2</u>, <u>Bcrypt</u> or <u>Scrypt</u>, typically use repeated invocations of a cryptographic hash to increase the time required to perform <u>brute force attacks</u> on stored password digests.

In 2013 a long-term <u>Password Hashing Competition</u> was announced to choose

Proof-of-work

Main article: <u>Proof-of-work system</u>

a new, standard algorithm for password hashing.

A proof-of-work system (or protocol, or function) is an economic measure to deter denial of service attacks and other service abuses such as spam on a network by requiring some work from the service requester, usually meaning processing time by a computer. A key feature of these schemes is their asymmetry: the work must be moderately hard (but feasible) on the requester side but easy to check for the service provider. One popular system — used in Bitcoin mining and Hashcash — uses partial hash inversions to prove that work was done, as a good-will token to send an e-mail. The sender is required to find a message whose hash value begins with a number of zero bits. The average work that sender needs to perform in order to find a valid message is exponential in the number of zero bits required in the hash value, while the

nonce

zero bits. The average work that sender needs to perform in order to find a valid message is exponential in the number of zero bits required in the hash value, while the recipient can verify the validity of the message by executing a single hash function. For instance, in Hashcash, a sender is asked to generate a header whose 160 bit SHA-1 hash value has the first 20 bits as zeros. The sender will *on average* have to try 2¹⁹ times to find a valid header.

$$202 = 1M$$

File or data identifier

A message digest can also serve as a means of reliably identifying a file; several source code management systems, including Git, Mercurial and Monotone, use the sha1sum of various types of content (file content, directory trees, ancestry information, etc.) to uniquely identify them. Hashes are used to identify files on peer-to-peer filesharing networks.

Pseudorandom generation and key derivation

Hash functions can also be used in the generation of <u>pseudorandom</u> bits, or to <u>derive new keys or passwords</u> from a single secure key or password.

As of 2009, the two most commonly used cryptographic hash functions were MD5 and SHA-1. However, a successful attack on MD5 broke Transport Layer Security in 2008.

In February 2005, an attack on SHA-1 was reported that would find <u>collision</u> in about 2⁶⁹ hashing operations, rather than the 2⁸⁰ expected for a 160-bit hash function. In August 2005, another attack on SHA-1 was reported that would find collisions in 2⁶³ operations. Though theoretical weaknesses of SHA-1 exist, [14][15] no collision (or near-collision) has yet been found. Nonetheless, it is often suggested that it may be practical to break within years, and that new applications can avoid these problems by using later members of the SHA family, such as <u>SHA-2</u>.

 $1k = 2^{10} = 1024$ $1M = 2^{20}$ $1G = 2^{30}$ $1T = 2^{40}$ 2^{112}

SHA-2 (Secure Hash Algorithm 2) is a set of <u>cryptographic hash</u> functions designed by the United States National Security Agency (NSA).[3]

From < https://en.wikipedia.org/wiki/SHA-2>

SHA-2 includes significant changes from its predecessor, SHA-1.

The SHA-2 family consists of six hash functions with digests (hash values) that are 224, 256, 384 or 512 bits:

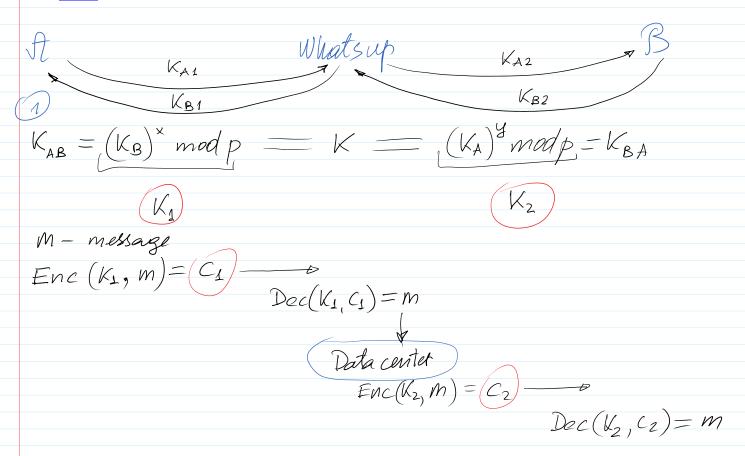
h28

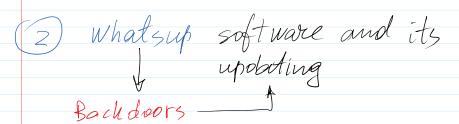
SHA-224, SHA-256, SHA-384, SHA-512, SHA-512/224, SHA-512/256.

However, to ensure the long-term robustness of applications that use hash functions, there was a <u>competition</u> to design a replacement for SHA-2.

On October 2, 2012, Keccak was selected as the winner of the <u>NIST</u> hash function competition.

A version of this algorithm became a <u>FIPS</u> standard on August 5, 2015 under the name <u>SHA-3</u>.





HMAC

Use in building other cryptographic primitives

Hash functions can be used to build other cryptographic primitives.

For these other primitives to be cryptographically secure, care must be taken to build them correctly.

Message authentication codes (MACs) (also called keyed hash functions) are often built from hash functions. HMAC is such a MAC.

Information

Authentication

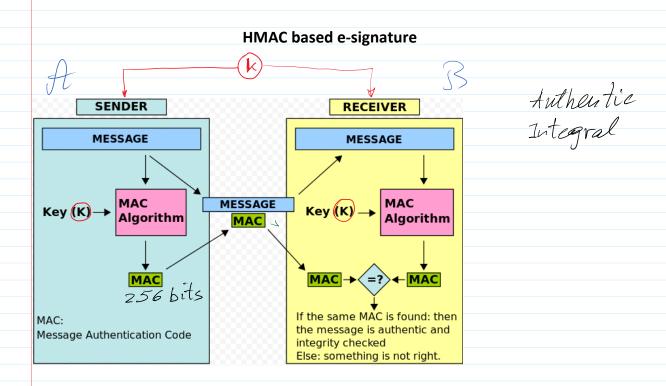
Integrity

Keyed-hash message authentication code (HMAC) is a specific type of message authentication code (MAC) involving a cryptographic hash function (hence the 'H') in combination with a secret cryptographic key.

As with any MAC it may be used to simultaneously varify both the data

As with any MAC, it may be used to simultaneously verify both the data integrity and the authentication of a message.

Any cryptographic hash function, may be used in the calculation of an HMAC. The cryptographic strength of the HMAC depends upon the cryptographic strength of the underlying hash function, the size of its hash output, and on the size and quality of the key.



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€ H26d	2019.10.26 14:30
€ h28	2020.03.22 17:08
€ H28d	2019.10.23 22:42
€ hd26	2020.03.22 17:08
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Hash functions based on block ciphers

There are several methods to use a block cipher to build a cryptographic hash function, specifically a one-way compression function.

The methods resemble the block cipher modes of operation usually used for encryption.

Many well-known hash functions, including MD4, MD5, SHA-1 and SHA-2 are built from block-cipher-like components

HMAC can be constructed form the block cipher using cipher block chaining (CBC) mode of operation.

CBC-MAC

 $AES_{k-}CBC$ M- to be signed.

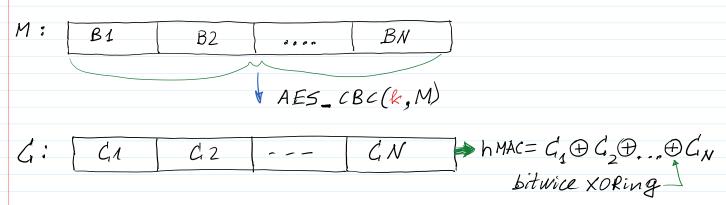
CBC-MAC

M - to be signed.

 $G = AES_CBC(k, M)$

Cipher block chaining message authentication code (CBC-MAC) is a technique for constructing a message authentication code from a block cipher. The message is encrypted with some block cipher algorithm in CBC mode to create a chain of blocks such that each block depends on the proper encryption of the previous block. This interdependence ensures that a change to any of the plaintext bits will cause the final encrypted block to change in a way that cannot be predicted or counteracted without knowing the key to the block cipher.

From < https://en.wikipedia.org/wiki/CBC-MAC>



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To calculate the CBC-MAC of message m one encrypts m in CBC mode with zero initialization vector.

The following figure sketches the computation of the CBC-MAC of a message comprising blocks using a secret key k and a block cipher E:

M-message to be hashed

k-secret enco. key

A(k) B(k)

A: wish to enco.

message m together wit providing its audhenticity and integrity.

Chosep Plaintext Attack f: $E_{csc}(k, m) = c$ encrypt $c_g h$ $B: DH_{csc}(k, e) = h'$ $H_{csc}(k, e) = h$ hash 2h + 2h' if ok

